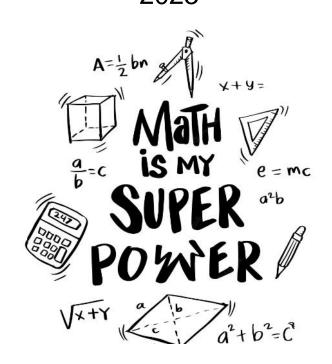
Myton School Mathematics A-Level Induction Pack 2023



Name:

Overview

Thank you for choosing to study Mathematics in the sixth form at Myton School. The Mathematics Department is committed to ensuring that you make good progress throughout your A-Level course. In order that you make the best possible start to the course, we have prepared this booklet.

Examinations:

Myton students follow the Edexcel exam board specification. Examinations happen at the end of Year 13 and cover all material covered.

This booklet takes you through all of the key information needed to prepare yourself for the course. It is crucial that you are familiar and confident with all the skills listed in this booklet.

You will have an induction test in September to check you understand the induction material.

Equipment:

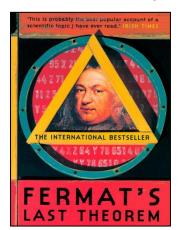
You will need a calculator for all of your lessons. We recommend the Casio fx-991 EX. This has all of the functions required for A Level.

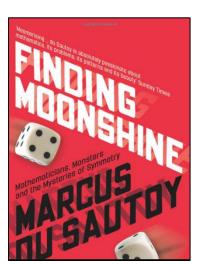
You are permitted in examinations to use the fx-CG50, a complex graphical calculator. This device has additional functions but is significantly more expensive and can be cumbersome to use.

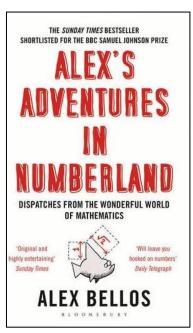
Alpha	Beta	Gamma	Delta
A a	Вβ	Γγ	Δδ
Epsilon	Zeta	Eta	Theta
Εε	Ζζ	Нη	Θθ
lota	Kappa	Lambda	Mu
H	Kκ	Λλ	Mμ
Nυ	Xi	Omicron	Pi
Νv	Ξξ	00	Пπ
Rho	Sigma	Tau	Upsilon
Ρρ	Σσ	Ττ	Yυ
Phi	Chi	Psi	Omega
Фφ	Хχ	ΨΨ	Ωω

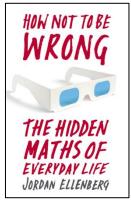
Recommended wider reading

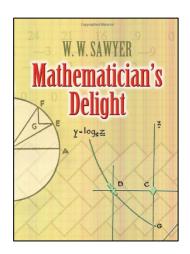
More available at https://nrich.maths.org/books

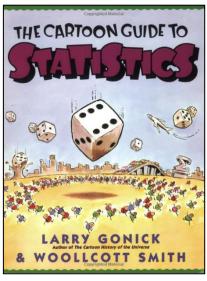


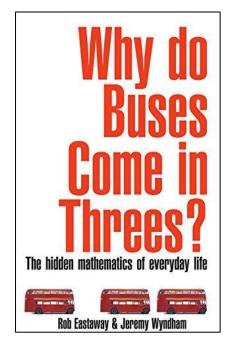














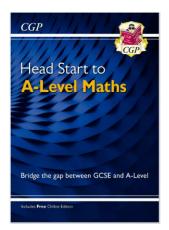
Pre course reading/homework

As you may be aware, two thirds of the A-Level course is comprised of Pure Maths and a heavy reliance is placed on your understanding of algebra and manipulation of numbers. To give you the maximum amount of lesson time on new topics, the following topics covered at GCSE are assumed knowledge and therefore not retaught in depth in Year 12.

- Index Laws
- Expanding Brackets
- Factorising linear and quadratic expressions
- Surd manipulation
- Rationalising the denominator
- Solving quadratics using factorising or the quadratic formula
- Completing the square
- Solving simultaneous equations
- Linear Inequalities

Your homework will be the revise these topics in detail before September. There is a transition workbook of questions for you to complete in addition to any individual work you undertake.

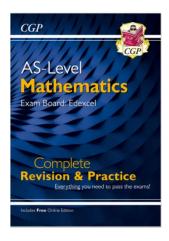
You may wish to purchase one of the following workbooks to help you, but this is not essential.



Head Start to A-Level Maths

ISBN: 9781782947929

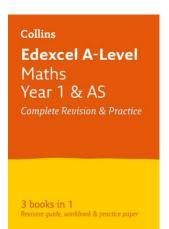
RRP: £5.95



AS-Level Maths Edexcel Complete Revision and Practice

ISBN: 9781782948049

RRP: £11.99



Edexcel Maths A Level Year 1 All-in-one Complete Revision and Practice

ISBN: 9780008268510

RRP: £12.99

Expectations

You will be expected to keep your lesson notes, examples and homework/tests organised in a folder with dividers.

You are expected to practise techniques learnt in class. As a rule of thumb, you should expect to do at least one hour of work out of class for every hour in class.

Recommended Resources for the A-Level Course

The following are free online resources which you may find helpful alongside studying the course from September.

- Maths Genie
- Physics and Maths Tutor
- Dr Frost Maths
- AMSP (Advanced Mathematics Support Programme) website
- Bicen Maths (YouTube)

Summer Learning

Here are some practice resources. You must be familiar with all of the following skills. Complete a selection of questions and mark using the answers at the back of the booklet. You do not have to complete every question.

Simplifying expressions

1 Simplify these expressions:

a
$$x^3 \times x^4$$

$$\chi^4$$

a
$$2p$$
 g $10x^5 \div 2x^3$

i
$$8p^4 \div 4p^3$$

$$\mathbf{m} \ 9x^2 \times 3(x^2)^3$$

p
$$(4y^3)^3 \div 2y^3$$

b $2x^3 \times 3x^2$

e
$$\frac{3x^3}{3x^2}$$

$$\mathbf{h} \ (p^3)^2 \div p^4$$

$$\mathbf{k} \ 2a^4 \times 3a^5$$

$$\mathbf{n} \ \ 3x^3 \times 2x^2 \times 4x^6$$

q
$$2a^3 \div 3a^2 \times 6a^5$$

 $\mathbf{c} = \frac{k^3}{k^2}$

f
$$(y^2)^5$$

i
$$(2a^3)^2 \div 2a^3$$

1
$$\frac{21a^3b^7}{7ab^4}$$

o
$$7a^4 \times (3a^4)^2$$

$$\mathbf{r} \quad 3a^4 \times 2a^5 \times a^3$$

2 Expand and simplify if possible:

a
$$9(x-2)$$

b
$$x(x + 9)$$

$$c -3y(4-3y)$$

d
$$x(y + 5)$$

$$e -x(3x + 5)$$

$$f -5x(4x + 1)$$

$$g (4x + 5)x$$

$$h -3v(5-2v^2)$$

h
$$-3y(5-2y^2)$$
 i $-2x(5x-4)$

$$\mathbf{j} (3x - 5)x^2$$

k
$$3(x+2) + (x-7)$$
 l $5x-6-(3x-2)$

1
$$5x - 6 - (3x - 2)$$

$$\mathbf{m} \ 4(c+3d^2) - 3(2c+d^2)$$
 $\mathbf{n} \ (r^2+3t^2+9) - (2r^2+3t^2-4)$

$$n (r^2 + 3t^2 + 9) - (2r^2 + 3t^2 + 9)$$

$$3t^2 - 4$$

o
$$x(3x^2 - 2x + 5)$$

$$\mathbf{p} \ 7y^2(2-5y+3y^2)$$

o
$$x(3x^2 - 2x + 5)$$
 p $7y^2(2 - 5y + 3y^2)$ **q** $-2y^2(5 - 7y + 3y^2)$

$$\mathbf{r}$$
 7(x - 2) + 3(x + 4) - 6(x - 2)

$$\mathbf{s} = 5x - 3(4 - 2x) + 6$$

$$t 3x^2 - x(3-4x) + 3$$

u
$$4x(x+3) - 2x(3x-7)$$

t
$$3x^2 - x(3-4x) + 7$$
 u $4x(x+3) - 2x(3x-7)$ v $3x^2(2x+1) - 5x^2(3x-4)$

3 Simplify these fractions:

a
$$\frac{6x^4 + 10x^6}{2x}$$

b
$$\frac{3x^5 - x^7}{x}$$

$$\frac{2x^4 - 4x^2}{4x}$$

d
$$\frac{8x^3 + 5x}{2x}$$

e
$$\frac{7x^7 + 5x^2}{5x}$$

6

$$f = \frac{9x^5 - 5x^3}{3x}$$

Expanding Brackets

1 Expand and simplify if possible:

a
$$(x+4)(x+7)$$

b
$$(x-3)(x+2)$$

c
$$(x-2)^2$$

d
$$(x-y)(2x+3)$$

e
$$(x + 3y)(4x - y)$$

$$f(2x-4y)(3x+y)$$

$$g(2x-3)(x-4)$$

h
$$(3x + 2y)^2$$

i
$$(2x + 8y)(2x + 3)$$

$$\mathbf{j} (x+5)(2x+3y-5)$$

$$k(x-1)(3x-4y-5)$$

k
$$(x-1)(3x-4y-5)$$
 l $(x-4y)(2x+y+5)$

$$\mathbf{m} (x + 2y - 1)(x + 3)$$
 $\mathbf{n} (2x + 2y + 3)(x + 6)$ $\mathbf{o} (4 - y)(4y - x + 3)$

$$n(2x+2v+3)(x+6)$$

$$0 (4-v)(4v-x+3)$$

p
$$(4y+5)(3x-y+2)$$
 q $(5y-2x+3)(x-4)$ **r** $(4y-x-2)(5-y)$

$$a (5y - 2x + 3)(x - 4)$$

$$r (4v - x - 2)(5 - v)$$

2 Expand and simplify if possible:

a
$$5(x+1)(x-4)$$

b
$$7(x-2)(2x+5)$$

c
$$3(x-3)(x-3)$$

d
$$x(x-y)(x+y)$$

e
$$x(2x + y)(3x + 4)$$
 f $y(x - 5)(x + 1)$

f
$$v(x-5)(x+1)$$

$$y(3x-2y)(4x+2)$$

h
$$y(7-x)(2x-5)$$

h
$$y(7-x)(2x-5)$$
 i $x(2x+y)(5x-2)$

Factorising

1 Factorise these expressions completely:

a
$$4x + 8$$

b
$$6x - 24$$

c
$$20x + 15$$

d
$$2x^2 + 4$$

e
$$4x^2 + 20$$

f
$$6x^2 - 18x$$

g
$$x^2 - 7x$$

h
$$2x^2 + 4x$$

i
$$3x^2 - x$$

i
$$6x^2 - 2x$$

$$k 10y^2 - 5y$$

1
$$35x^2 - 28x$$

$$m x^2 + 2x$$

n
$$3v^2 + 2v$$

o
$$4x^2 + 12x$$

p
$$5y^2 - 20y$$

$$q 9xy^2 + 12x^2y$$

r
$$6ab - 2ab^2$$

s
$$5x^2 - 25xy$$

$$t 12x^2y + 8xy^2$$

u
$$15y - 20yz^2$$

$$v 12x^2 - 30$$

$$\mathbf{w} xy^2 - x^2y$$

$$x 12y^2 - 4yx$$

2 Factorise:

a
$$x^2 + 4x$$

b
$$2x^2 + 6x$$

$$\mathbf{c} \quad x^2 + 11x + 24$$

d
$$x^2 + 8x + 12$$

e
$$x^2 + 3x - 40$$

f
$$x^2 - 8x + 12$$

$$\mathbf{g} \ x^2 + 5x + 6$$

h
$$x^2 - 2x - 24$$

i
$$x^2 - 3x - 10$$

j
$$x^2 + x - 20$$

$$\mathbf{k} \ 2x^2 + 5x + 2$$

1
$$3x^2 + 10x - 8$$

m
$$5x^2 - 16x + 3$$

o $2x^2 + 7x - 15$

n
$$6x^2 - 8x - 8$$

$$\mathbf{p} \ 2x^4 + 14x^2 + 24$$

$$\mathbf{q} \ x^2 - 4$$

$$\mathbf{r} \quad x^2 - 49$$

u
$$36x^2 - 4$$

$$4x^2 - 25$$

$$t 9x^2 - 25y^2$$

$$v 2x^2 - 50$$

$$\mathbf{w} 6x^2 - 10x + 4$$

$$\mathbf{x} = 15x^2 + 42x - 9$$

Indices

1 Simplify:

a
$$x^3 \div x^{-2}$$

d
$$(x^2)^{\frac{3}{2}}$$

g
$$9x^{\frac{2}{3}} \div 3x^{\frac{1}{6}}$$

$$\mathbf{j} \quad \sqrt{x} \times \sqrt[3]{x}$$

b
$$x^5 \div x^7$$

e
$$(x^3)^{\frac{5}{3}}$$

h
$$5x^{\frac{7}{5}} \div x^{\frac{2}{5}}$$

$$\mathbf{k} \ (\sqrt{x})^3 \times (\sqrt[3]{x})^4$$

$$\mathbf{c} \quad x^{\frac{3}{2}} \times x^{\frac{5}{2}}$$

f
$$3x^{0.5} \times 4x^{-0.5}$$

i
$$3x^4 \times 2x^{-5}$$

$$1 \quad \frac{(\sqrt[3]{x})^2}{\sqrt{x}}$$

2 Evaluate:

a
$$25^{\frac{1}{2}}$$

$$d 4^{-2}$$

$$g (\frac{3}{4})^0$$

j
$$\left(\frac{27}{8}\right)^{\frac{2}{3}}$$

b
$$81^{\frac{3}{2}}$$

e
$$9^{-\frac{1}{2}}$$

h
$$1296^{\frac{3}{4}}$$

$$k \left(\frac{6}{5}\right)^{-1}$$

c
$$27^{\frac{1}{3}}$$

$$f (-5)^{-3}$$

f
$$(-5)^{-3}$$
i $(\frac{25}{16})^{\frac{3}{2}}$

$$\left(\frac{343}{512}\right)^{-\frac{2}{3}}$$

Surds

1 Do not use your calculator for this exercise. Simplify:

a
$$\sqrt{28}$$

b
$$\sqrt{72}$$

$$\mathbf{c} = \sqrt{50}$$

$$\mathbf{d} \sqrt{32}$$

$$\mathbf{f} = \frac{\sqrt{12}}{2}$$

$$g \frac{\sqrt{27}}{3}$$

h
$$\sqrt{20} + \sqrt{80}$$

i
$$\sqrt{200} + \sqrt{18} - \sqrt{72}$$

$$\sqrt{175} + \sqrt{63} + 2\sqrt{28}$$

$$k \sqrt{28} - 2\sqrt{63} + \sqrt{7}$$

1
$$\sqrt{80} - 2\sqrt{20} + 3\sqrt{45}$$

$$\mathbf{m} \ 3\sqrt{80} - 2\sqrt{20} + 5\sqrt{45}$$

$$n \frac{\sqrt{44}}{\sqrt{11}}$$

$$\mathbf{o} \quad \sqrt{12} + 3\sqrt{48} + \sqrt{75}$$

2 Expand and simplify if possible:

a
$$\sqrt{3}(2+\sqrt{3})$$

b
$$\sqrt{5}(3-\sqrt{3})$$

c
$$\sqrt{2}(4-\sqrt{5})$$

d
$$(2-\sqrt{2})(3+\sqrt{5})$$

e
$$(2-\sqrt{3})(3-\sqrt{7})$$
 f $(4+\sqrt{5})(2+\sqrt{5})$

f
$$(4+\sqrt{5})(2+\sqrt{5})$$

g
$$(5-\sqrt{3})(1-\sqrt{3})$$

h
$$(4+\sqrt{3})(2-\sqrt{3})$$

i
$$(7 - \sqrt{11})(2 + \sqrt{11})$$

1 Simplify:

a
$$\frac{1}{\sqrt{5}}$$

b
$$\frac{1}{\sqrt{11}}$$

c
$$\frac{1}{\sqrt{2}}$$

d
$$\frac{\sqrt{3}}{\sqrt{15}}$$

e
$$\frac{\sqrt{12}}{\sqrt{48}}$$

$$\mathbf{f} \quad \frac{\sqrt{5}}{\sqrt{80}}$$

$$g \frac{\sqrt{12}}{\sqrt{156}}$$

$$h \ \frac{\sqrt{7}}{\sqrt{63}}$$

2 Rationalise the denominators and simplify:

$$\mathbf{a} \ \frac{1}{1+\sqrt{3}}$$

b
$$\frac{1}{2+\sqrt{5}}$$

c
$$\frac{1}{3-\sqrt{7}}$$

d
$$\frac{4}{3-\sqrt{5}}$$

a
$$\frac{1}{1+\sqrt{3}}$$
 b $\frac{1}{2+\sqrt{5}}$ **c** $\frac{1}{3-\sqrt{7}}$ **d** $\frac{4}{3-\sqrt{5}}$ **e** $\frac{1}{\sqrt{5}-\sqrt{3}}$

f
$$\frac{3-\sqrt{2}}{4-\sqrt{5}}$$

$$\mathbf{g} \ \frac{5}{2+\sqrt{5}}$$

h
$$\frac{5\sqrt{2}}{\sqrt{8}-\sqrt{7}}$$

i
$$\frac{11}{3 + \sqrt{11}}$$

f
$$\frac{3-\sqrt{2}}{4-\sqrt{5}}$$
 g $\frac{5}{2+\sqrt{5}}$ **h** $\frac{5\sqrt{2}}{\sqrt{8}-\sqrt{7}}$ **i** $\frac{11}{3+\sqrt{11}}$ **j** $\frac{\sqrt{3}-\sqrt{7}}{\sqrt{3}+\sqrt{7}}$

$$\mathbf{k} \frac{\sqrt{17} - \sqrt{11}}{\sqrt{17} + \sqrt{11}}$$

$$k \ \frac{\sqrt{17} - \sqrt{11}}{\sqrt{17} + \sqrt{11}} \qquad \qquad l \ \frac{\sqrt{41} + \sqrt{29}}{\sqrt{41} - \sqrt{29}} \qquad \qquad m \ \frac{\sqrt{2} - \sqrt{3}}{\sqrt{3} - \sqrt{2}}$$

$$\mathbf{m} \frac{\sqrt{2} - \sqrt{3}}{\sqrt{3} - \sqrt{2}}$$

Factorising

1 Solve the following equations using factorisation:

$$\mathbf{a} \ \ x^2 + 3x + 2 = 0$$

b
$$x^2 + 5x + 4 = 0$$

a
$$x^2 + 3x + 2 = 0$$
 b $x^2 + 5x + 4 = 0$ **c** $x^2 + 7x + 10 = 0$ **d** $x^2 - x - 6 = 0$

d
$$x^2 - x - 6 = 0$$

$$e^{-}x^2 - 8x + 15 = 0$$

$$\mathbf{f} \ \ x^2 - 9x + 20 = 0$$

$$\mathbf{g} \ x^2 - 5x - 6 = 0$$

e
$$x^2 - 8x + 15 = 0$$
 f $x^2 - 9x + 20 = 0$ **g** $x^2 - 5x - 6 = 0$ **h** $x^2 - 4x - 12 = 0$

2 Solve the following equations using factorisation:

a
$$x^2 = 4x$$

b
$$x^2 = 25x$$

c
$$3x^2 = 6x$$

c
$$3x^2 = 6x$$
 d $5x^2 = 30x$

$$e \ 2x^2 + 7x + 3 = 0$$

$$\mathbf{f} \ 6x^2 - 7x - 3 = 0$$

$$\mathbf{g} = 6x^2 - 5x - 6 = 0$$

e
$$2x^2 + 7x + 3 = 0$$
 f $6x^2 - 7x - 3 = 0$ **g** $6x^2 - 5x - 6 = 0$ **h** $4x^2 - 16x + 15 = 0$

Solving quadratics

1 Solve the following equations using the quadratic formula. Give your answers exactly, leaving them in surd form where necessary.

$$\mathbf{a} \ \ x^2 + 3x + 1 = 0$$

b
$$x^2 - 3x - 2 = 0$$

a
$$x^2 + 3x + 1 = 0$$
 b $x^2 - 3x - 2 = 0$ **c** $x^2 + 6x + 6 = 0$

d
$$x^2 - 5x - 2 = 0$$

e
$$3x^2 + 10x - 2 = 0$$
 f $4x^2 - 4x - 1 = 0$

$$\mathbf{f} \ 4x^2 - 4x - 1 = 0$$

$$\mathbf{g} \ 4x^2 - 7x = 2$$

h
$$11x^2 + 2x - 7 = 0$$

Solving simultaneous equations

1 Solve these simultaneous equations by elimination:

a
$$2x - y = 6$$

$$4x + 3y = 22$$

b
$$7x + 3y = 16$$

 $2x + 9y = 29$

c
$$5x + 2y = 6$$

 $3x - 10y = 26$

d
$$2x - y = 12$$

$$6x + 2y = 21$$

e
$$3x - 2y = -6$$

$$6x + 3y = 2$$

2 Solve these simultaneous equations by substitution:

a
$$x + 3y = 11$$

 $4x - 7y = 6$

b
$$4x - 3y = 40$$

 $2x + y = 5$

c
$$3x - y = 7$$
 d $2y = 2x - 3$ $10x + 3y = -2$ $3y = x - 1$

$$\mathbf{d} \quad 2y = 2x - 3$$
$$3y = x - 1$$

1 Solve the simultaneous equations:

$$\mathbf{a} \quad x + y = 11$$
$$xy = 30$$

b
$$2x + y = 1$$

 $x^2 + y^2 = 1$

$$\mathbf{c} \quad y = 3x$$
$$2y^2 - xy = 15$$

2 Solve the simultaneous equations:

a
$$2x + 2y = 7$$

 $x^2 - 4y^2 = 8$

b
$$x + y = 9$$

 $x^2 - 3xy + 2y^2 = 0$

c
$$5y - 4x = 1$$

 $x^2 - y^2 + 5x = 41$

Gradient

Work out the gradients of the lines joining these pairs of points:

b
$$(-1, 3), (5, 4)$$

$$\mathbf{d}$$
 (2, -3), (6, 5)

$$e(-3, 4), (7, -6)$$

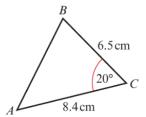
h
$$(\frac{1}{2}, 2), (\frac{3}{4}, 4)$$

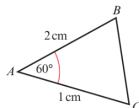
f (-12, 3), (-2
i
$$(\frac{1}{4}, \frac{1}{2}), (\frac{1}{2}, \frac{2}{3})$$

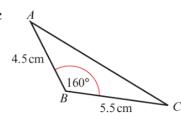
Cosine Rule

1 In each of the following triangles calculate the length of the missing side.

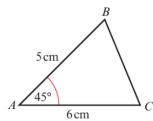
a

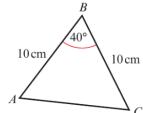


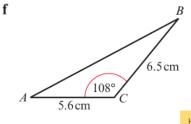




d

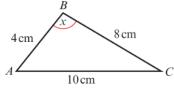


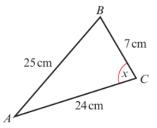




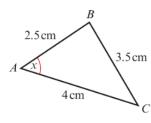
2 In the following triangles calculate the size of the angle marked x:

a

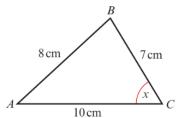




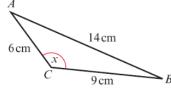
c



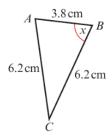
d



 \mathbf{e}

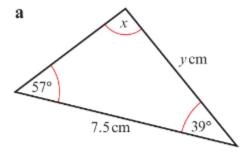


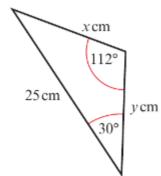
 \mathbf{f}

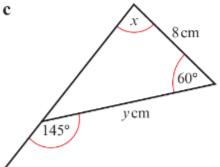


Sine Rule

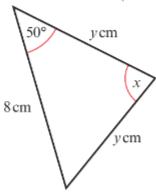
2 In each of the following triangles calculate the values of x and y.

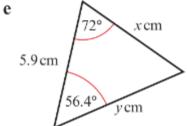




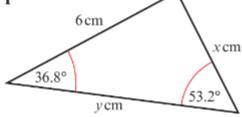


d





f



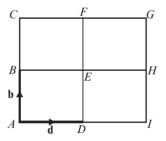
Vectors

2 ACGI is a square, B is the midpoint of AC, F is the midpoint of CG, H is the midpoint of GI, D is the midpoint of AI.

 $\overrightarrow{AB} = \mathbf{b}$ and $\overrightarrow{AD} = \mathbf{d}$. Find, in terms of \mathbf{b} and \mathbf{d} :

- $\overrightarrow{a} \overrightarrow{AC}$
- **b** \overrightarrow{BE}
- $\overrightarrow{\mathbf{r}}$
- $d \overline{DF}$

- $\begin{array}{ccc}
 \mathbf{e} & \overrightarrow{AE} \\
 \mathbf{i} & \overrightarrow{AH}
 \end{array}$
- $\overrightarrow{\mathbf{f}} \quad \overrightarrow{DH}$ $\overrightarrow{\mathbf{i}} \quad \overrightarrow{BI}$
- $\mathbf{g} \quad \overrightarrow{HB}$ $\mathbf{k} \quad \overrightarrow{EI}$
- $1 \overline{FE}$



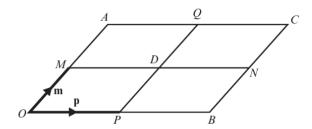
3 *OACB* is a parallelogram. *M*, *Q*, *N* and *P* are the midpoints of *OA*, *AC*, *BC* and *OB* respectively.

Vectors \mathbf{p} and \mathbf{m} are equal to \overrightarrow{OP} and \overrightarrow{OM} respectively. Express in terms of \mathbf{p} and \mathbf{m} .

- \overrightarrow{oA}
- **b** \overrightarrow{OB}
- \overrightarrow{BN}
- $\mathbf{d} \ \overrightarrow{DQ}$

- $\overrightarrow{e} \overrightarrow{OD}$
- $\overrightarrow{\mathbf{f}} \stackrel{\partial D}{\overrightarrow{MQ}}$
- \overrightarrow{OQ}
- \overrightarrow{h} \overrightarrow{AD}

- \overrightarrow{CD}
- $\overrightarrow{\mathbf{j}}$ \overrightarrow{AP}
- $\mathbf{k} \stackrel{\longrightarrow}{BM}$
- $1 \overline{N}$



Summer Learning Solutions

Simplifying expressions

- 2 a 9x 18 b $x^2 + 9x$ c $-12y + 9y^2$ d xy + 5xe $-3x^2 - 5x$ f $-20x^2 - 5x$ g $4x^2 + 5x$ h $-15y + 6y^3$ i $-10x^2 + 8x$ j $3x^3 - 5x^2$ k 4x - 1 l 2x - 4m $9d^2 - 2c$ n $13 - r^2$ o $3x^3 - 2x^2 + 5x$ p $14y^2 - 35y^3 + 21y^4$ q $-10y^2 + 14y^3 - 6y^4$ r 4x + 10s 11x - 6 t $7x^2 - 3x + 7$ u $-2x^2 + 26x$ v $-9x^3 + 23x^2$
- 3 **a** $3x^3 + 5x^5$ **b** $3x^4 x^6$ **c** $\frac{x^3}{2} x$ **d** $4x^2 + \frac{5}{2}$ **e** $\frac{7x^6}{5} + x$ **f** $3x^4 \frac{5x^2}{3}$

Expanding Brackets

1 **a**
$$x^2 + 11x + 28$$

b $x^2 - x - 6$
c $x^2 - 4x + 4$

d
$$2x^2 + 3x - 2xy - 3y$$

e
$$4x^2 + 11xy - 3y^2$$

f
$$6x^2 - 10xy - 4y^2$$

g
$$2x^2 - 11x + 12$$

h $9x^2 + 12xy + 4y^2$

i
$$4x^2 + 6x + 16xy + 24y$$

$$\mathbf{j} = 2x^2 + 3xy + 5x + 15y - 25$$

$$\mathbf{k} \quad 3x^2 - 4xy - 8x + 4y + 5$$

1
$$2x^2 + 5x - 7xy - 4y^2 - 20y$$

$$\mathbf{m} \ x^2 + 2x + 2xy + 6y - 3$$

$$\mathbf{n} \quad 2x^2 + 15x + 2xy + 12y + 18$$

$$\mathbf{o} \quad 13y - 4x + 12 - 4y^2 + xy$$

$$\mathbf{p} = 12xy - 4y^2 + 3y + 15x + 10$$

$$\mathbf{q} = 5xy - 20y - 2x^2 + 11x - 12$$

$$\mathbf{r} = 22y - 4y^2 - 5x + xy - 10$$

2 **a**
$$5x^2 - 15x - 20$$

b
$$14x^2 + 7x - 70$$

$$\mathbf{c} = 3x^2 - 18x + 27$$

d
$$x^3 - xy^2$$

$$e 6x^3 + 8x^2 + 3x^2y + 4xy$$

$$f x^2y - 4xy - 5y$$

$$\mathbf{g} \quad 12x^2y + 6xy - 8xy^2 - 4y^2$$

h
$$19xy - 35y - 2x^2y$$

i
$$10x^3 - 4x^2 + 5x^2y - 2xy$$

Factorising

1 **a**
$$4(x+2)$$

c
$$5(4x + 3)$$

e
$$4(x^2 + 5)$$

$$\mathbf{g} \quad x(x-7)$$

i
$$x(3x - 1)$$

k
$$5y(2y-1)$$

m
$$x(x + 2)$$

o
$$4x(x + 3)$$

q
$$3xy(3y+4x)$$

$$\mathbf{s} \quad 5x(x-5y)$$

u
$$5y(3-4z^2)$$

$$\mathbf{w} \ xy(y-x)$$

b
$$6(x-4)$$

d
$$2(x^2 + 2)$$

$$\mathbf{f} = 6x(x-3)$$

h
$$2x(x + 2)$$

j
$$2x(3x-1)$$

1
$$7x(5x-4)$$

n
$$y(3y + 2)$$

p
$$5y(y-4)$$

r
$$2ab(3-b)$$

$$\mathbf{t} = 4xy(3x + 2y)$$

$$\mathbf{v} = 6(2x^2 - 5)$$

$$\mathbf{x} \quad 4y(3y-x)$$

2 **a**
$$x(x + 4)$$

c
$$(x + 8)(x + 3)$$

e
$$(x + 8)(x - 5)$$

$$g(x+2)(x+3)$$

i
$$(x-5)(x+2)$$

$$k (2x + 1)(x + 2)$$

$$\mathbf{m} (5x - 1)(x - 3)$$

o
$$(2x-3)(x+5)$$

q
$$(x+2)(x-2)$$

$$s (2x + 5)(2x - 5)$$

u
$$4(3x+1)(3x-1)$$

$$\mathbf{w} \ \ 2(3x-2)(x-1)$$

b
$$2x(x+3)$$

d
$$(x+6)(x+2)$$

$$f(x-6)(x-2)$$

h
$$(x-6)(x+4)$$

$$\mathbf{i}$$
 $(x+5)(x-4)$

$$1 (3x-2)(x+4)$$

$$n 2(3x+2)(x-2)$$

$$\mathbf{p} = 2(x^2 + 3)(x^2 + 4)$$

$$\mathbf{r}$$
 $(x+7)(x-7)$

$$t (3x + 5y)(3x - 5y)$$

$$\mathbf{v} = 2(x+5)(x-5)$$

$$\mathbf{x} = 3(5x - 1)(x + 3)$$

Indices

1 a
$$x^5$$

$$\mathbf{e} \quad x^5$$

i
$$6x^{-1}$$

b
$$x^{-2}$$

f
$$12x^0 = 12$$
 g $3x^{\frac{1}{2}}$

$$12x^0 = 12$$

$$\mathbf{j} \quad x^{\frac{5}{6}}$$

b 729

$$\mathbf{c}$$
 x^4

g
$$3x^{\frac{1}{2}}$$

$$\mathbf{k} \quad x^{\frac{17}{6}}$$

d
$$x^3$$

$$1 \quad x^{\frac{1}{6}}$$

i

$$\mathbf{k} = \frac{5}{6}$$

d
$$\frac{1}{16}$$

$$1 \frac{64}{49}$$

Surds

1 **a**
$$2\sqrt{7}$$

b
$$6\sqrt{2}$$

$$c \quad 5\sqrt{2}$$

d
$$4\sqrt{2}$$

$$e 3\sqrt{10}$$

 $\frac{125}{64}$

$$f \quad \sqrt{3}$$

$$\mathbf{g} = \sqrt{3}$$

$$h \quad 6\sqrt{5}$$

i
$$7\sqrt{2}$$

j
$$12\sqrt{7}$$

$$\mathbf{k} - 3\sqrt{7}$$

1
$$9\sqrt{5}$$

$$m\ 23\sqrt{5}$$

o
$$19\sqrt{3}$$

2 **a**
$$2\sqrt{3} + 3$$

c
$$4\sqrt{2} - \sqrt{10}$$

e
$$6 - 2\sqrt{7} - 3\sqrt{3} + \sqrt{21}$$
 f $13 + 6\sqrt{5}$

g
$$8 - 6\sqrt{3}$$

i
$$3 + 5\sqrt{11}$$

b
$$3\sqrt{5} - \sqrt{15}$$

d
$$6 + 2\sqrt{5} - 3\sqrt{2} - \sqrt{10}$$

f
$$13 + 6\sqrt{5}$$

h
$$5 - 2\sqrt{3}$$

1 **a**
$$\frac{\sqrt{5}}{5}$$
 b $\frac{\sqrt{11}}{11}$ **c** $\frac{\sqrt{2}}{2}$ **d** $\frac{\sqrt{5}}{5}$

$$e \frac{1}{2}$$

$$\mathbf{f} = \frac{1}{4}$$

e
$$\frac{1}{2}$$
 f $\frac{1}{4}$ g $\frac{\sqrt{13}}{13}$ h $\frac{1}{3}$

h
$$\frac{1}{3}$$

2 a
$$\frac{1-\sqrt{3}}{-2}$$
 b $\sqrt{5}-2$ **c** $\frac{3+\sqrt{7}}{2}$

b
$$\sqrt{5}$$
 – 2

$$\mathbf{c} \quad \frac{3+\sqrt{7}}{2}$$

d
$$3 + \sqrt{5}$$

$$\mathbf{e} \quad \frac{\sqrt{5} + \sqrt{3}}{2}$$

d
$$3 + \sqrt{5}$$
 e $\frac{\sqrt{5} + \sqrt{3}}{2}$ **f** $\frac{(3 - \sqrt{2})(4 + \sqrt{5})}{11}$

g
$$5(\sqrt{5}-2)$$

h
$$5(4 + \sqrt{14})$$

g
$$5(\sqrt{5}-2)$$
 h $5(4+\sqrt{14})$ **i** $\frac{11(3-\sqrt{11})}{-2}$

j
$$\frac{5-\sqrt{21}}{-2}$$

$$k \frac{14 - \sqrt{187}}{3}$$

j
$$\frac{5-\sqrt{21}}{-2}$$
 k $\frac{14-\sqrt{187}}{3}$ **l** $\frac{35+\sqrt{1189}}{6}$

m - 1

Factorising

1 **a**
$$x = -1$$
 or $x = -2$

$$x = -5 \text{ or } x = -2$$

e
$$x = 3 \text{ or } x = 5$$

$$\mathbf{g} \ \ x = 6 \text{ or } x = -1$$

b
$$x = -1$$
 or $x = -4$

d
$$x = 3 \text{ or } x = -2$$

f
$$x = 4 \text{ or } x = 5$$

h
$$x = 6$$
 or $x = -2$

2 a
$$x = 0$$
 or $x = 4$

c
$$x = 0 \text{ or } x = 2$$

e
$$x = -\frac{1}{2}$$
 or $x = -3$

$$\mathbf{g} \quad x = -\frac{2}{3} \text{ or } x = \frac{3}{2}$$

b
$$x = 0$$
 or $x = 25$

d
$$x = 0 \text{ or } x = 6$$

f
$$x = -\frac{1}{3}$$
 or $x = \frac{3}{2}$

h
$$x = \frac{3}{2}$$
 or $x = \frac{5}{2}$

Solving quadratics

1 **a**
$$x = \frac{1}{2} \left(-3 \pm \sqrt{5} \right)$$

$$\mathbf{c} \quad x = -3 \pm \sqrt{3}$$

e
$$x = \frac{1}{3}(-5 \pm \sqrt{31})$$

g
$$x = 2 \text{ or } x = -\frac{1}{4}$$

b
$$x = \frac{1}{2}(3 \pm \sqrt{17})$$

d
$$x = \frac{1}{2}(5 \pm \sqrt{33})$$

f
$$x = \frac{1}{2}(1 \pm \sqrt{2})$$

h
$$x = \frac{1}{11}(-1 \pm \sqrt{78})$$

Solving simultaneous equations

1 **a**
$$x = 4, y = 2$$

c
$$x = 2, y = -2$$

$$e \quad x = -\frac{2}{3}, y = 2$$

a
$$x = 5, y = 2$$

c
$$x = 1, y = -4$$

b
$$x = 1, y = 3$$

d
$$x = 4\frac{1}{2}, y = -3$$

f
$$x = 3, y = 3$$

b
$$x = 5\frac{1}{2}, y = -6$$

d
$$x = 1\frac{3}{4}, y = \frac{1}{4}$$

1 **a**
$$x = 5, y = 6 \text{ or } x = 6, y = 5$$

b
$$x = 0, y = 1 \text{ or } x = \frac{4}{5}, y = -\frac{3}{5}$$

$$\mathbf{c}$$
 $x = -1, y = -3 \text{ or } x = 1, y = 3$

2 a
$$x = 3$$
, $y = \frac{1}{2}$ or $x = 6\frac{1}{3}$, $y = -2\frac{5}{6}$

b
$$x = 4\frac{1}{2}$$
, $y = 4\frac{1}{2}$ or $x = 6$, $y = 3$

$$\mathbf{c}$$
 $x = -19, y = -15 \text{ or } x = 6, y = 5$

Gradient

2

1 **a**
$$\frac{1}{2}$$

1 **a**
$$\frac{1}{2}$$
 b $\frac{1}{6}$ **c** $-\frac{3}{5}$ **d** 2
e -1 **f** $\frac{1}{2}$ **g** $\frac{1}{2}$ **h** 8
i $\frac{2}{3}$ **j** -4 **k** $-\frac{1}{3}$ **l** $-\frac{2}{3}$

$$\mathbf{i} = \frac{2}{3}$$

$$\mathbf{b} = \frac{1}{6}$$

$$oldsymbol{b} = rac{1}{6}$$

$$\mathbf{g} = \frac{1}{2}$$

$$\frac{8}{k} - \frac{1}{2}$$

$$1 -\frac{1}{2}$$

Cosine Rule

1a $3.19 \, \mathrm{cm}$ b $1.73 \, \mathrm{cm} \, (\sqrt{3} \, \mathrm{cm})$ c $9.85 \, \mathrm{cm}$ d4.31 cme $6.84 \, \mathrm{cm}$ f $9.80 \, \mathrm{cm}$

2 **a** 108(.2)° **b** 90° **c** 60° **d** 52.6° **e** 137° **f** 72.2°

Sine Rule

2 **a**
$$x = 84^{\circ}, y = 6.32$$

b $x = 13.5, y = 16.6$
c $x = 85^{\circ}, y = 13.9$
d $x = 80^{\circ}, y = 6.22$ (isosceles triangle)
e $x = 6.27, y = 7.16$
f $x = 4.49, y = 7.49$ (right-angled)

Vectors